

## FORMULARIO

### TRIGONOMETRIA

$$\sin^2 x + \cos^2 x = 1; \quad \tan x = \frac{\sin x}{\cos x}; \quad \coth x = \frac{\cos x}{\sin x}$$

$$\begin{aligned} \sin(-x) &= -\sin x; \quad \cos(-x) = \cos x; \quad \sin(\frac{\pi}{2} \pm x) = \cos x; \quad \cos(\frac{\pi}{2} \pm x) = \mp \sin x; \\ \sin(\pi \pm x) &= \mp \sin x; \quad \cos(\pi \pm x) = -\cos x; \quad \sin(x + 2\pi) = \sin x; \quad \cos(x + 2\pi) = \cos x; \end{aligned}$$

$$\sin(x \pm y) = \sin x \cos y \pm \cos x \sin y; \quad \cos(x \pm y) = \cos x \cos y \mp \sin x \sin y$$

$$\begin{aligned} \sin(2x) &= 2 \sin x \cos x; \quad \cos(2x) = \cos^2 x - \sin^2 x = 2 \cos^2 x - 1 = 1 - 2 \sin^2 x \\ \cos^2 x &= \frac{1+\cos(2x)}{2}; \quad \sin^2 x = \frac{1-\cos(2x)}{2} \end{aligned}$$

$$\begin{aligned} \sin u + \sin v &= 2 \sin \frac{u+v}{2} \cos \frac{u-v}{2}; \quad \sin u - \sin v = 2 \cos \frac{u+v}{2} \sin \frac{u-v}{2}; \quad \cos u + \cos v = 2 \cos \frac{u+v}{2} \cos \frac{u-v}{2}; \\ \cos u - \cos v &= -2 \sin \frac{u+v}{2} \sin \frac{u-v}{2}; \end{aligned}$$

$$\begin{aligned} \sin x \cos y &= \frac{1}{2} [\sin(x+y) + \sin(x-y)]; \quad \cos x \cos y = \frac{1}{2} [\cos(x+y) + \cos(x-y)]; \\ \sin x \sin y &= -\frac{1}{2} [\cos(x+y) - \cos(x-y)] \end{aligned}$$

$$\text{Posto } t = \tan(x/2), \text{ si ha: } \sin x = \frac{2t}{1+t^2}; \quad \cos x = \frac{1-t^2}{1+t^2}; \quad \tan x = \frac{2t}{1-t^2};$$

$$\begin{aligned} \sin 0 &= 0 & \cos 0 &= 1 & \sin \frac{\pi}{6} &= \frac{1}{2}; & \cos \frac{\pi}{6} &= \frac{\sqrt{3}}{2}; & \sin \frac{\pi}{4} &= \frac{\sqrt{2}}{2}; & \cos \frac{\pi}{4} &= \frac{\sqrt{2}}{2}; \\ \sin \frac{\pi}{3} &= \frac{\sqrt{3}}{2}; & \sin \frac{\pi}{3} &= \frac{1}{2}; & \sin \frac{\pi}{2} &= 1; & \cos \frac{\pi}{2} &= 0; \end{aligned}$$

### DISUGUAGLIANZE

$$|\sin x| \leq |x| \text{ per ogni } x \in \mathbb{R}; \quad 0 \leq 1 - \cos x \leq \frac{x^2}{2} \text{ per ogni } x \in \mathbb{R};$$

$$\log(1+x) \leq x \text{ per ogni } x > -1; \quad |xy| \leq \frac{x^2+y^2}{2}; \quad \frac{(x+y)^2}{2} \leq x^2 + y^2; \quad x^4 + y^4 \leq (x^2 + y^2)^2$$

### SVILUPPI DI MACLAURIN

$$e^x = 1 + x + \frac{x^2}{2!} + \frac{x^3}{3!} + \cdots + \frac{x^n}{n!} + o(x^n)$$

$$\log(1+x) = x - \frac{x^2}{2} + \frac{x^3}{3} + \cdots + (-1)^{n+1} \frac{x^n}{n} + o(x^n)$$

$$\sin x = x - \frac{x^3}{3!} + \frac{x^5}{5!} + \cdots + (-1)^n \frac{x^{2n+1}}{(2n+1)!} + o(x^{2n+2})$$

$$\cos x = 1 - \frac{x^2}{2!} + \frac{x^4}{4!} + \cdots + (-1)^n \frac{x^{2n}}{2n!} + o(x^{2n+1})$$

$$\tan x = x + \frac{1}{3}x^3 + \frac{2}{15}x^5 + o(x^6)$$

$$\arctan x = x - \frac{x^3}{3} + \frac{x^5}{5} + \cdots + (-1)^n \frac{x^{2n+1}}{2n+1} + o(x^{2n+2})$$

$$(1+x)^\alpha = 1 + \alpha x + \frac{\alpha(\alpha-1)}{2!} x^2 + \frac{\alpha(\alpha-1)(\alpha-2)}{3!} x^3 + \cdots + \frac{\alpha(\alpha-1)\cdots(\alpha-n+1)}{n!} x^n + o(x^n)$$