

Solution

$$\textcircled{1} \quad E_t = E_{ot} = E_0 \cos \beta$$

$$\epsilon_2 E_n = E_{on} \rightarrow E_n = \frac{E_0}{\epsilon_2} \sin \beta$$

$$\nabla_p = P_n = \epsilon_0 \chi E_n = \epsilon_0 \frac{\epsilon_2 - 1}{\epsilon_2} E_0 \sin \beta$$

$$\textcircled{2} \quad d\vec{B} = \frac{\mu_0}{4\pi} I \frac{d\vec{l} \times \Delta\vec{r}}{|\Delta\vec{r}|^3}$$

$$B_{AB} = B_{CD} = 0$$

$$B_{DA} = \frac{\mu_0}{4\pi} \left(\frac{I}{b} \right) \int_0^{\pi b} dl = \frac{\mu_0 I}{4b}$$

$$B_{BC} = - \frac{\mu_0}{4\pi} \frac{I}{a} \int_0^{\pi a} dl = - \frac{\mu_0 I}{4a}$$

$$B_{\text{TOT}} = \frac{\mu_0 I}{4} \left(\frac{1}{b} - \frac{1}{a} \right) = -2.1 \cdot 10^{-5} \text{ T}$$

$$\textcircled{3} \quad I_L(t=0) = \frac{f}{R+R_0} = \frac{f}{2R}$$

$$\Delta V_c(t=0) = I_L(t=0) \cdot R_0$$

$$\left\{ \begin{array}{l} U_L^i = \frac{1}{2} L I_L^2(t=0) \end{array} \right.$$

$$\left\{ \begin{array}{l} U_c^i = \frac{1}{2} C \Delta V_c^2(t=0) \end{array} \right.$$

$$\boxed{U_J^f = U_L^i + U_c^i}$$

$$C = 2 \frac{U_J^f - U_L^i}{\Delta V_c^2(t=0)} = 10^{-7} \text{ F}$$

$$\textcircled{4} \quad \text{Faraday: } E_{2\pi r} = -\frac{dB}{dt} \pi a^2$$

$$E = -\frac{d}{dt} [\mu_0 n I_0 \sin(\omega t)] \frac{a^2}{2r} =$$

$$= -\mu_0 n I_0 \omega \frac{a^2}{2r} \cos(\omega t)$$

\hat{t} versor tang. elle circulaire.

$$\vec{P} = \epsilon_0 \chi \vec{E} = -\hat{t} \mu_0 \epsilon_0 (\epsilon_2 - 1) n I_0 \omega \frac{a^2}{2r} \cos(\omega t)$$

$$\textcircled{5} \quad \vec{I} = \frac{6}{10^{-4} \cdot 60} = 1 \frac{\text{KW}}{\text{m}^2}$$

$$E_0 = \sqrt{2 Z_0 I} = 868 \frac{\text{V}}{\text{m}}$$

$$B_0 = \frac{E_0}{c} = 2.9 \cdot 10^{-6} \frac{\text{Wb}}{\text{m}^2}$$